

PhysicsByAaryan

CSIR NET . GATE . JEST . BARC - Physics

Canonical Ensemble - CSIR NET Physics PYQs

Statistical Mechanics . All PYQs (2015-2025) with answer key

36 questions . Answer key included

www.physicsbyaaryan.com . www.csirnetphysics.com

Contact: 9501976811

Q1. [Dec 2015] . 3.5 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2015 Dec	3.5 M
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For a system of independent non interacting one-dimensional oscillators, the value of the free energy per oscillator, in the limit $T \rightarrow 0$, is

1. $\frac{1}{2} \hbar \omega$
2. $\hbar \omega$
3. $\frac{3}{2} \hbar \omega$
4. 0

Q2. [Dec 2015] . 3.5 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2015 Dec	3.5 M
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The Hamiltonian of a system of N non interacting spin $-\frac{1}{2}$ particles is $H = -\mu_0 B \sum_i S_i^Z$, where $S_i^Z = \pm 1$ are components of i^{th} spin along an external magnetic field B . At a temperature T such that $e^{\frac{\mu_0 B}{k_B T}} = 2$. the specific heat per particle is

1. $\frac{16}{25} k_B$
2. $\frac{8}{25} k_B \ln 2$
3. $k_B (\ln 2)^2$
4. $\frac{16}{25} k_B (\ln 2)^2$

Q3. [Dec 2015] . 5.0 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2015 Dec	5 M
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An ensemble of non-interacting spin $-\frac{1}{2}$ particles is in contact with a heat bath at temperature T and is subjected to an external magnetic field. Each particle can be in one of the two quantum states of energies $\pm\epsilon_0$. If the mean energy per particle is $-\epsilon_0/2$, then the free energy per particle is

1. $-2 \epsilon_0 \frac{\ln(4/\sqrt{3})}{\ln 3}$

2. $-\epsilon_0 \ln(3/2)$

3. $-2 \epsilon_0 \ln 2$

4. $-\epsilon_0 \frac{\ln 2}{\ln 3}$

Q4. [June 2015] . 3.5 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2015 June	3.5 M
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A system of N non-interacting classical particles, each of mass m is in a two dimensional harmonic potential of the form $V(r) = \alpha(x^2 + y^2)$ where α is a positive constant. The canonical partition function of the system at temperature T is

$$\left(\beta = \frac{1}{k_B T}\right):$$

1. $\left[\left(\frac{\alpha}{2m}\right)^2 \frac{\pi}{\beta}\right]^N$
2. $\left(\frac{2m\pi}{\alpha\beta}\right)^{2N}$
3. $\left(\frac{\alpha\pi}{2m\beta}\right)^N$
4. $\left(\frac{2m\pi^2}{\alpha\beta^2}\right)^N$

Q5. [Dec 2016] . 3.5 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2016 Dec	3.5M
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The partition function of a two-level system

governed by the Hamiltonian $H = \begin{bmatrix} \gamma & -\delta \\ -\delta & -\gamma \end{bmatrix}$ is

1. $2\sinh(\beta\sqrt{\gamma^2 + \delta^2})$

2. $2\cosh(\beta\sqrt{\gamma^2 + \delta^2})$

3. $\frac{1}{2} \left[\cosh(\beta\sqrt{\gamma^2 + \delta^2}) + \sinh(\beta\sqrt{\gamma^2 + \delta^2}) \right]$

4. $\frac{1}{2} \left[\cosh(\beta\sqrt{\gamma^2 + \delta^2}) - \sinh(\beta\sqrt{\gamma^2 + \delta^2}) \right]$

Q6. [Dec 2016] . 5.0 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2016 Dec	5M
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An atom has a non-degenerate ground-state and a doubly-degenerate excited state. The energy difference between the two states is ε . The specific heat at very low temperatures ($\beta\varepsilon \gg 1$) is given by

1. $k_B(\beta\varepsilon)$

2. $k_B e^{-\beta\varepsilon}$

3. $2k_B(\beta\varepsilon)^2 e^{-\beta\varepsilon}$

4. k_B

Q7. [June 2016] . 3.5 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2016 June	3.5M
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A gas of non-relativistic classical particles in one dimension is subjected to a potential $V(x) = \alpha|x|$ (where α is a constant). The partition function is

$$\left(\beta = \frac{1}{k_B T} \right)$$

1. $\sqrt{\frac{4m\pi}{\beta^3 \alpha^2 h^2}}$

2. $\sqrt{\frac{2m\pi}{\beta^3 \alpha^2 h^2}}$

3. $\sqrt{\frac{8m\pi}{\beta^3 \alpha^2 h^2}}$

4. $\sqrt{\frac{3m\pi}{\beta^3 \alpha^2 h^2}}$

Q8. [June 2016] . 5.0 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2016 June	5M
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The internal energy $E(T)$ of a system at a fixed volume is found to depend on the temperature T as $E(T) = aT^2 + bT^4$. Then the entropy $S(T)$, as a function of temperature, is

1. $\frac{1}{2}aT^2 + \frac{1}{4}bT^4$

2. $2aT^2 + 4bT^4$

3. $2aT + \frac{4}{3}bT^3$

4. $2aT + 2bT^3$

Q9. [Dec 2017] . 5.0 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2017 Dec	5M
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A closed system having three non-degenerate energy levels with energies $E = 0, \pm\epsilon$, is at temperature T . For $\epsilon = 2k_B T$, the probability of finding the system in the state with energy $E = 0$, is

1. $\frac{1}{(1+2\cosh 2)}$
2. $\frac{1}{(2\cosh 2)}$
3. $\frac{1}{2} \cosh 2$
4. $\frac{1}{\cosh 2}$

Q10. [Dec 2017] . 5.0 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2017 Dec	5M
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Two non-degenerate energy levels with energies 0 and ϵ are occupied by N noninteracting particles at a temperature T . Using classical statistics, the average internal energy of the system is

1. $\frac{N\epsilon}{(1+e^{\epsilon/k_B T})}$
2. $\frac{N\epsilon}{(1-e^{\epsilon/k_B T})}$
3. $N \epsilon e^{-\epsilon/k_B T}$
4. $\frac{3}{2} N k_B T$

Q11. [Dec 2018] . 3.5 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2018 Dec	3.5M
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The rotational energy levels of a molecule are $E_\ell = \frac{\hbar^2}{2I_0} \ell(\ell + 1)$, where $\ell = 0, 1, 2, \dots$ and I_0 is its moment of inertia. The contribution of the rotational motion to the Helmholtz free energy per molecule, at low temperatures in a dilute gas of these molecules, is approximately

1. $-k_B T \left(1 + \frac{\hbar^2}{I_0 k_B T} \right)$

2. $-k_B T e^{-\frac{\hbar^2}{I_0 k_B T}}$

3. $-k_B T$

4. $-3k_B T e^{-\frac{\hbar^2}{I_0 k_B T}}$

Q12. [Dec 2018] . 3.5 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2018 Dec	3.5M
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The vibrational motion of a diatomic molecule may be considered to be that of a simple harmonic oscillator with angular frequency ω . If a gas of these molecules is at temperature T , what is the probability that a randomly picked molecule will be found in its lowest vibrational state?

1. $1 - e^{-\frac{\hbar\omega}{k_B T}}$

2. $e^{-\frac{\hbar\omega}{2k_B T}}$

3. $\tanh\left(\frac{\hbar\omega}{k_B T}\right)$

4. $\frac{1}{2} \operatorname{cosech}\left(\frac{\hbar\omega}{2k_B T}\right)$

Q13. [Dec 2018] . 5.0 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2018 Dec	5M
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The energy levels accessible to a molecule have energies $E_1 = 0, E_2 = \Delta$ and $E_3 = 2\Delta$ (where Δ is a constant). A gas of these molecules is in thermal equilibrium at temperature T . The specific heat at constant volume in the high temperature limit ($k_B T \gg \Delta$) varies with temperature as

1. $\frac{1}{T^{3/2}}$

2. $\frac{1}{T^3}$

3. $\frac{1}{T}$

4. $\frac{1}{T^2}$

Q14. [June 2018] . 3.5 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2018 June	3.5M
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In a system of N distinguishable particles, each particle can be in one of two states with energies 0 and $-E$, respectively. The mean energy of the system at temperature T is

1. $-\frac{1}{2}N(1 + e^{\varepsilon/k_B T})$

2. $-NE(1 + e^{\varepsilon/k_B T})$

3. $-\frac{1}{2}NE$

4. $-NE(1 + e^{-\varepsilon/k_B T})$

Q15. [Dec 2019] . 3.5 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2019 Dec	3.5M
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The angular frequency of oscillation of a quantum harmonic oscillator in two dimensions is ω . If it is in contact with an external heat bath at temperature T , its partition function is (in the following $\beta = \frac{1}{k_B T}$)

1.
$$\frac{e^{2\beta\hbar\omega}}{(e^{2\beta\hbar\omega} - 1)^2}$$

2.
$$\frac{e^{\beta\hbar\omega}}{(e^{\beta\hbar\omega} - 1)^2}$$

3.
$$\frac{e^{\beta\hbar\omega}}{e^{\beta\hbar\omega} - 1}$$

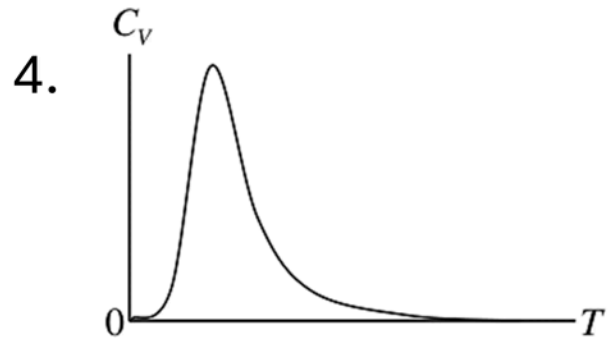
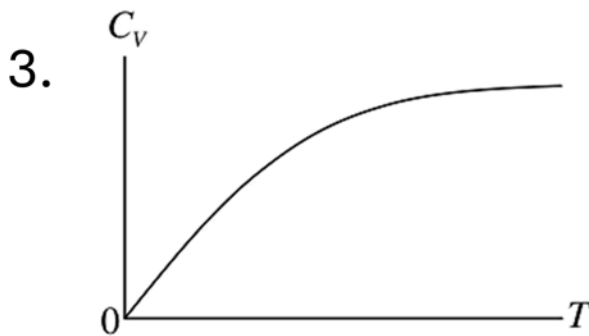
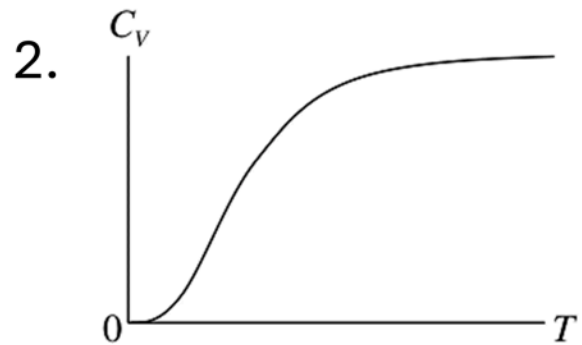
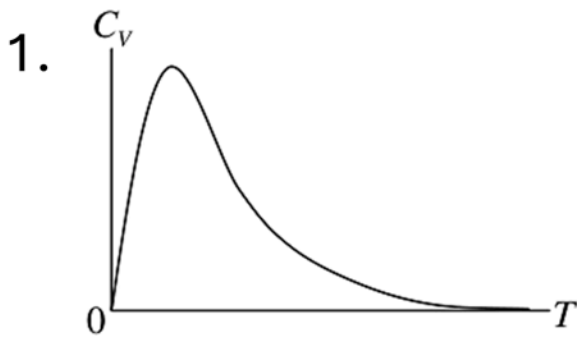
4.
$$\frac{e^{2\beta\hbar\omega}}{e^{2\beta\hbar\omega} - 1}$$

Q16. [Dec 2019] . 3.5 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2019 Dec	3.5M
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The energies available to a three state system are $0, E$ and $2E$, where $E > 0$. Which of the following graphs best represents the temperature dependence of the specific heat?



Q17. [Dec 2019] . 5.0 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2019 Dec	5M
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For a crystal, let ϕ denote the energy required to create a pair of vacancy and interstitial defects. If n pairs of such defects are formed, and $n \ll N, N'$, where N and N' are respectively, the total number of lattice and interstitial sites, then n is approximately

1. $\sqrt{NN'} e^{-\phi/(2k_B T)}$
2. $\sqrt{NN'} e^{-\phi/(k_B T)}$
3. $\frac{1}{2} (N + N') e^{-\phi/(2k_B T)}$
4. $\frac{1}{2} (N + N') e^{-\phi/(k_B T)}$

Q18. [Dec 2019] . 5.0 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2019 Dec	5M
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The Hamiltonian of two particles, each of mass m ,

$$\text{is } H(q_1, p_1; q_2, p_2) = \frac{p_1^2}{2m} + \frac{p_2^2}{2m} + k \left(q_1^2 + q_2^2 + \frac{1}{4} q_1 q_2 \right),$$

where $k > 0$ is a constant. The value of the partition function

$$Z(\beta)$$

$$= \int_{-\infty}^{\infty} dq_1 \int_{-\infty}^{\infty} dp_1 \int_{-\infty}^{\infty} dq_2 \int_{-\infty}^{\infty} dp_2 e^{-\beta H(q_1, p_1; q_2, p_2)} \text{ is}$$

$$1. \frac{2m\pi^2}{k\beta^2} \sqrt{\frac{16}{15}}$$

$$2. \frac{2m\pi^2}{k\beta^2} \sqrt{\frac{15}{16}}$$

$$3. \frac{2m\pi^2}{k\beta^2} \sqrt{\frac{63}{64}}$$

$$4. \frac{2m\pi^2}{k\beta^2} \sqrt{\frac{64}{63}}$$

Q19. [June 2020] . 3.5 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2020 June	3.5M
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An idealised atom has a non-degenerate ground state at zero energy and a g -fold degenerate excited state of energy E . In a non-interacting system of N such atoms, the population of the excited state may exceed that of the ground state above a

temperature $T > \frac{E}{2k_B \ln 2}$. The minimum value of g for which this is possible is

1. 8
2. 4
3. 2
4. 1

Q20. [June 2021] . 5.0 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2021 June	5M
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The energy levels of a non-degenerate quantum system are $\epsilon_n = nE_0$, where E_0 is a constant and $n = 1, 2, 3, \dots$. At a temperature T , the free energy F can be expressed in terms of the average energy E by

1. $E_0 + k_B T \ln \frac{E}{E_0}$

2. $E_0 + 2k_B T \ln \frac{E}{E_0}$

3. $E_0 - k_B T \ln \frac{E}{E_0}$

4. $E_0 - 2k_B T \ln \frac{E}{E_0}$

Q21. [June 2021] . 5.0 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2021 June	5M
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A polymer, made up of N monomers, is in thermal equilibrium at temperature T . Each monomer could be of length a or $2a$. The first contributes zero energy, while the second one contributes ϵ . The average length (in units of Na) of the polymer at temperature $T = \epsilon/k_B$ is

1. $\frac{5+e}{4+e}$
2. $\frac{4+e}{3+e}$
3. $\frac{3+e}{2+e}$
4. $\frac{2+e}{1+e}$

Q22. [June 2022] . 3.5 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2022 June	3.5M
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If the average energy $\langle E \rangle_T$ of a quantum harmonic oscillator at a temperature T is such that $\langle E \rangle_T = 2\langle E \rangle_{T \rightarrow 0}$, then T satisfies

1. $\coth\left(\frac{\hbar\omega}{k_B T}\right) = 2$
2. $\coth\left(\frac{\hbar\omega}{2k_B T}\right) = 2$
3. $\coth\left(\frac{\hbar\omega}{k_B T}\right) = 4$
4. $\coth\left(\frac{\hbar\omega}{2k_B T}\right) = 4$

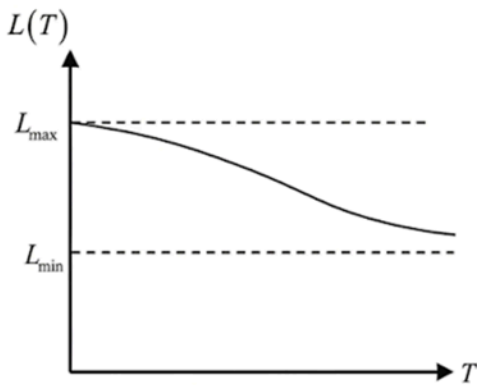
Q23. [June 2022] . 3.5 marks

Statistical Mechanics > Canonical Ensemble

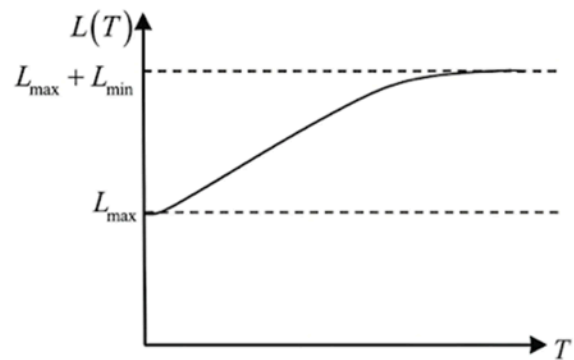
CSIR NET	2022 June	3.5M
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An elastic rod has a low energy state of length L_{\max} and high energy state of length L_{\min} . The best schematic representation of the temperature (T) dependence of the mean equilibrium length $L(T)$ of the rod, is

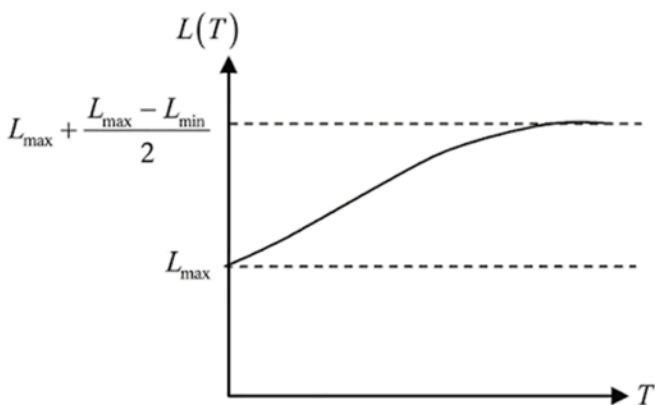
1.



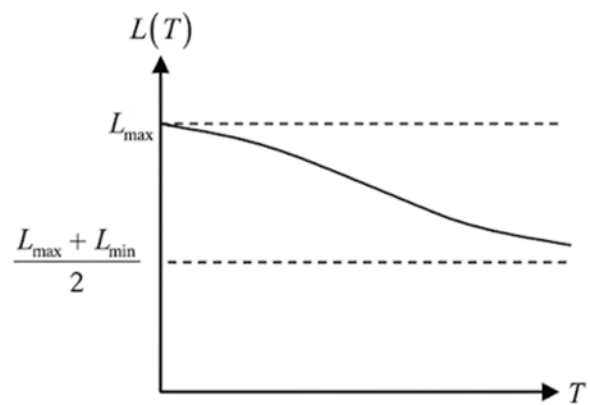
2.



3.



4.



Q24. [June 2022] . 5.0 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2022 June	5M
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The energy levels of a system, which is in equilibrium at temperature $T = 1/(k_B\beta)$, are $0, \epsilon$ and 2ϵ . If two identical bosons occupy these energy levels, the probability of the total energy being 3ϵ , is

1. $\frac{e^{-3\beta\epsilon}}{1+e^{-\beta\epsilon}+e^{-2\beta\epsilon}+e^{-3\beta\epsilon}+e^{-4\beta\epsilon}}$
2. $\frac{e^{-3\beta\epsilon}}{1+2e^{-\beta\epsilon}+2e^{-2\beta\epsilon}+e^{-3\beta\epsilon}+e^{-4\beta\epsilon}}$
3. $\frac{e^{-3\beta\epsilon}}{e^{-\beta\epsilon}+2e^{-2\beta\epsilon}+e^{-3\beta\epsilon}+e^{-4\beta\epsilon}}$
4. $\frac{e^{-3\beta\epsilon}}{1+e^{-\beta\epsilon}+2e^{-2\beta\epsilon}+e^{-3\beta\epsilon}+e^{-4\beta\epsilon}}$

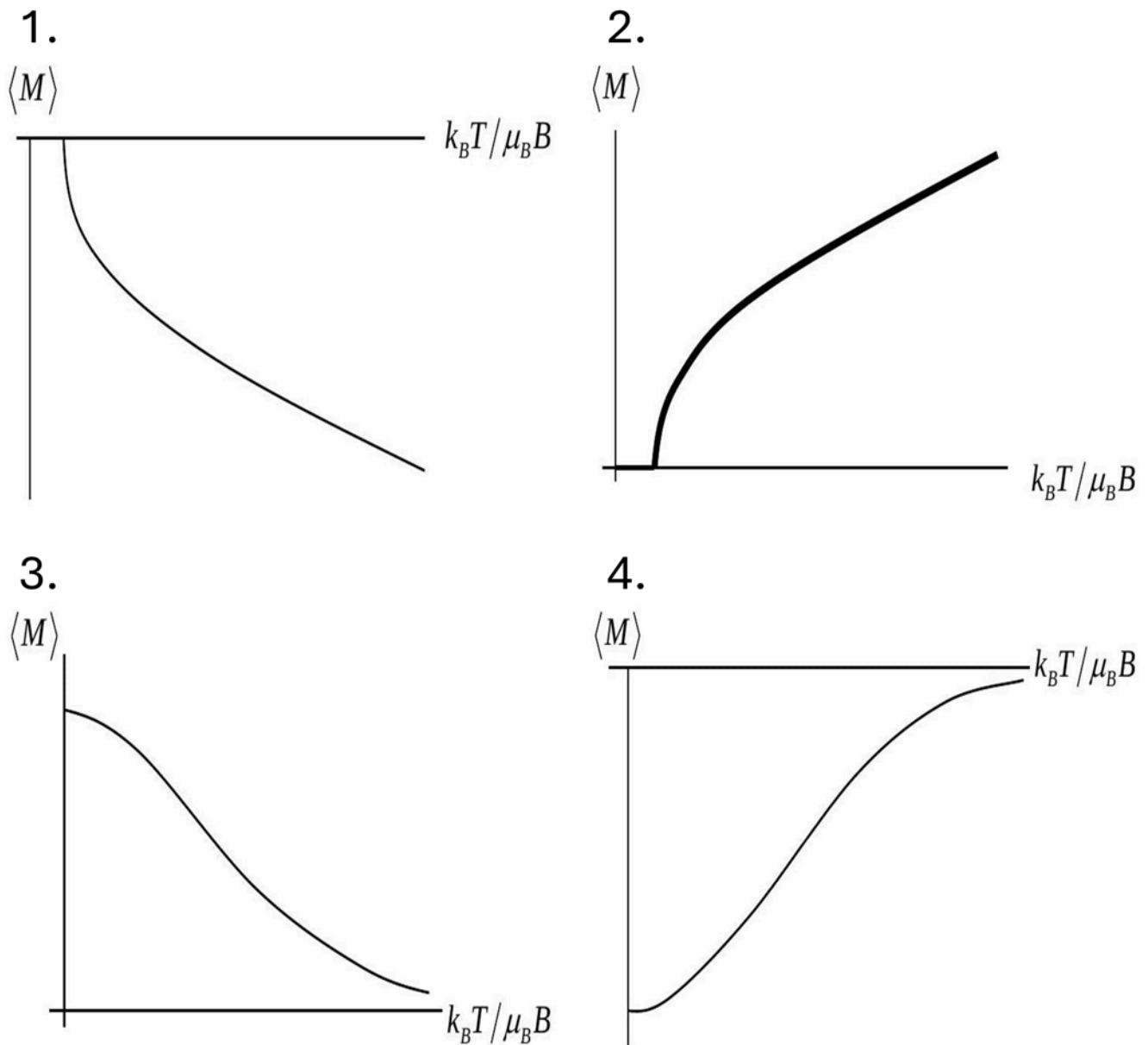
Q25. [June 2022] . 5.0 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2022 June	5M
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A paramagnetic salt with magnetic moment per ion $\mu_{\pm} = \pm\mu_B$ (where μ_B is the Bohr magneton) is in thermal equilibrium at temperature T in a constant magnetic field B . The average magnetic moment

$\langle M \rangle$, as a function of $\frac{k_B T}{\mu_B B}$, is best represented by



Q26. [June 2022] . 5.0 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2022 June	5M
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The energies of a two-level system are $\pm E$. Consider an ensemble of such non-interacting systems at a temperature T . At low temperatures, the leading term in the specific heat depends on T as

1. $\frac{1}{T^2} e^{-E/k_B T}$
2. $\frac{1}{T^2} e^{-2E/k_B T}$
3. $T^2 e^{-E/k_B T}$
4. $T^2 e^{-2E/k_B T}$

Q27. [Dec 2023] . 3.5 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2023 Dec	3.5 M
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A quantum system is described by the Hamiltonian

$$H = JS_z + \lambda S_x$$

where $S_i = \frac{\hbar}{2} \sigma_i$ and $\sigma_i (i = x, y, z)$ are the Pauli matrices. If $0 < \lambda \ll J$, then the leading correction in λ to the partition function of the system at temperature T is

1. $\frac{\hbar\lambda^2}{2Jk_B T} \coth\left(\frac{J\hbar}{2k_B T}\right)$
2. $\frac{\hbar\lambda^2}{2Jk_B T} \tanh\left(\frac{J\hbar}{2k_B T}\right)$
3. $\frac{\hbar\lambda^2}{2Jk_B T} \cosh\left(\frac{J\hbar}{2k_B T}\right)$
4. $\frac{\hbar\lambda^2}{2Jk_B T} \sinh\left(\frac{J\hbar}{2k_B T}\right)$

Q28. [Dec 2023] . 3.5 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2023 Dec	3.5 M
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A system of N non-interacting classical spins, where each spin can take values $\sigma = -1, 0, 1$, is placed in a magnetic field h . The single spin Hamiltonian is given by

$$H = -\mu_B h \sigma + \Delta(1 - \sigma^2),$$

where μ_B, Δ are positive constants with appropriate dimensions. If M is the magnetization, the zero-field magnetic susceptibility per spin $\frac{1}{N} \frac{\partial M}{\partial h} \Big|_{h \rightarrow 0}$, at a temperature $T = 1/\beta k_B$ is given by

1. $\beta \mu_B^2$
2. $\frac{2\beta \mu_B^2}{2 + e^{-\beta \Delta}}$
3. $\beta \mu_B^2 e^{-\beta \Delta}$
4. $\frac{\beta \mu_B^2}{1 + e^{-\beta \Delta}}$

Q29. [June 2023] . 5.0 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2023 June	5M
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Two electrons in thermal equilibrium at temperature $T = k_B/\beta$ can occupy two sites. The energy of the configuration in which they occupy the different sites is $J\mathbf{S}_1 \cdot \mathbf{S}_2$ (where $J > 0$ is a constant and \mathbf{S} denotes the spin of an electron), while it is U if they are at the same site. If $U = 10J$, the probability for the system to be in the first excited state is

1. $e^{-3\beta J/4} / (3e^{\beta J/4} + e^{-3\beta J/4} + 2e^{-10\beta J})$
2. $3e^{-\beta J/4} / (3e^{-\beta J/4} + e^{3\beta J/4} + 2e^{-10\beta J})$
3. $e^{-\beta J/4} / (2e^{-\beta J/4} + 3e^{3\beta J/4} + 2e^{-10\beta J})$
4. $3e^{-3\beta J/4} / (2e^{\beta J/4} + 3e^{-3\beta J/4} + 2e^{-10\beta J})$

Q30. [Dec 2024] . 3.5 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2024 Dec	3.5M
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A system comprises of N distinguishable atoms ($N \gg 1$). Each atom has two energy levels ω and 3ω ($\omega > 0$). Let ε_{eq} denote the average energy per particle when the system is in thermal equilibrium, the upper limit of ε_{eq} is

1. $\frac{3\omega}{2}$
2. 3ω
3. $\frac{5\omega}{2}$
4. 2ω

Q31. [June 2024] . 3.5 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2024 June	3.5M
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Quantum particles of unit mass, in a potential

$$V(x) = \begin{cases} \frac{1}{2} \omega^2 x^2 & x > 0 \\ \infty & x \leq 0 \end{cases}$$

are in equilibrium at a temperature T . Let n_2 and n_3 denote the numbers of the particles in the second and third excited states respectively. The ratio n_2/n_3 is given by

1. $\exp\left(\frac{2\hbar\omega}{k_B T}\right)$
2. $\exp\left(\frac{\hbar\omega}{k_B T}\right)$
3. $\exp\left(\frac{3\hbar\omega}{k_B T}\right)$
4. $\exp\left(\frac{4\hbar\omega}{k_B T}\right)$

Q32. [June 2024] . 3.5 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2024 June	3.5M
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A single particle can exist in two states with energies 0 and E respectively. At high temperatures ($k_B T \gg E$) the specific heat of the system (C_V) will be approximately

1. proportional to $\frac{1}{T}$
2. proportional to $\frac{1}{T^2}$
3. proportional to $e^{\frac{E}{k_B T}}$
4. constant

Q33. [Dec 2025] . 3.5 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2025 Dec	3.5M	Stat. Mech.
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Five indistinguishable atoms are sitting on the distinguishable vertices of a pentagon. The atoms can be in one of the two states: g with energy 0 , and e with energy E . However neighboring atoms cannot both be in the e state. The partition function of this system at temperature T , is

1. $1 + 5e^{-\frac{E}{k_B T}} + 2e^{-\frac{2E}{k_B T}}$

2. $1 + 5e^{-\frac{E}{k_B T}} + 3e^{-\frac{2E}{k_B T}}$

3. $1 + 5e^{-\frac{E}{k_B T}} + 10e^{-\frac{2E}{k_B T}}$

4. $1 + 5e^{-\frac{E}{k_B T}} + 5e^{-\frac{2E}{k_B T}}$

Q34. [Dec 2025] . 5.0 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2025 Dec	5M	Stat. Mech.
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Consider a one-dimensional lattice (with lattice spacing a) along X -axis with sites labelled by $x = 0, 1, 2, \dots, L$. A particle carrying a charge $-q$ can occupy any one of these sites. An electric field of strength E is applied in the positive x-direction. The average energy of the particle at a temperature T (in the limit $L \rightarrow \infty$) is $\left(\beta = \frac{1}{k_B T}\right)$

1. $\frac{Eq a}{e^{\beta Eq a} - 1}$

2. $\frac{Eq a}{1 + e^{\beta Eq a}}$

3. $\frac{Eq a}{2}$

4. $-Eq a$

Q35. [June 2025] . 5.0 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2025 June	5M	Stat. Mech.
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A rigid molecule can have two possible rotational states: $j = 0$ or $j = 1$. Its rotational energies are given by $\epsilon_j = \frac{\hbar^2}{2I} j(j + 1)$, where I is its moment of inertia. For an ensemble of such molecules in thermal equilibrium at temperature T , the ratio of the number of molecules in the $j = 1$ state (N_1), to those in $j = 0$ state (N_0), is $\frac{N_1}{N_0} = 0.003$. The temperature T (in units of $\frac{\hbar^2}{2Ik_B}$, where k_B is the Boltzmann constant) is closest to

1. 0.29 2. 0.21 3. 0.15 4. 0.34

Q36. [June 2025] . 5.0 marks

Statistical Mechanics > Canonical Ensemble

CSIR NET	2025 June	5M	Stat. Mech.
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A thermodynamic system (at temperature T and volume V), is described by its internal energy

$U = AT^4V$ and pressure $p = \frac{1}{3}AT^4$, where A is a constant of appropriate dimension. The Helmholtz free energy of the system is

1. $\frac{4}{3}AT^4V$
2. $\frac{1}{3}AT^4V$
3. $-\frac{1}{3}AT^4V$
4. $-\frac{4}{3}AT^4V$

Answer Key

36 questions . Subject and topic for quick revision

Q. No	Subject	Topic	Answer
Q1	Statistical Mechanics	Canonical Ensemble	1
Q2	Statistical Mechanics	Canonical Ensemble	4
Q3	Statistical Mechanics	Canonical Ensemble	1
Q4	Statistical Mechanics	Canonical Ensemble	4
Q5	Statistical Mechanics	Canonical Ensemble	2
Q6	Statistical Mechanics	Canonical Ensemble	3
Q7	Statistical Mechanics	Canonical Ensemble	3
Q8	Statistical Mechanics	Canonical Ensemble	3
Q9	Statistical Mechanics	Canonical Ensemble	1
Q10	Statistical Mechanics	Canonical Ensemble	1
Q11	Statistical Mechanics	Canonical Ensemble	4
Q12	Statistical Mechanics	Canonical Ensemble	1
Q13	Statistical Mechanics	Canonical Ensemble	4
Q14	Statistical Mechanics	Canonical Ensemble	4
Q15	Statistical Mechanics	Canonical Ensemble	2
Q16	Statistical Mechanics	Canonical Ensemble	4
Q17	Statistical Mechanics	Canonical Ensemble	1
Q18	Statistical Mechanics	Canonical Ensemble	4
Q19	Statistical Mechanics	Canonical Ensemble	2
Q20	Statistical Mechanics	Canonical Ensemble	3
Q21	Statistical Mechanics	Canonical Ensemble	4
Q22	Statistical Mechanics	Canonical Ensemble	2
Q23	Statistical Mechanics	Canonical Ensemble	4
Q24	Statistical Mechanics	Canonical Ensemble	4
Q25	Statistical Mechanics	Canonical Ensemble	3
Q26	Statistical Mechanics	Canonical Ensemble	2
Q27	Statistical Mechanics	Canonical Ensemble	4
Q28	Statistical Mechanics	Canonical Ensemble	2
Q29	Statistical Mechanics	Canonical Ensemble	2
Q30	Statistical Mechanics	Canonical Ensemble	4
Q31	Statistical Mechanics	Canonical Ensemble	1
Q32	Statistical Mechanics	Canonical Ensemble	2
Q33	Statistical Mechanics	Canonical Ensemble	4
Q34	Statistical Mechanics	Canonical Ensemble	1
Q35	Statistical Mechanics	Canonical Ensemble	1
Q36	Statistical Mechanics	Canonical Ensemble	3

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