

# PhysicsByAaryan

CSIR NET . GATE . JEST . BARC - Physics

## Basic Quantum Mechanics - CSIR NET Physics PYQs

Quantum Mechanics . All PYQs (2015-2025) with answer key

**36 questions . Answer key included**

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## Q1. [Dec 2015] . 3.5 marks

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2015 Dec	3.5 M
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A Hermitian operator  $\hat{O}$  has two normalized eigenstates  $|1\rangle$  and  $|2\rangle$  with eigenvalues 1 and 2, respectively. The two states

$|u\rangle = \cos \theta |1\rangle + \sin \theta |2\rangle$  and  $|v\rangle = \cos \phi |1\rangle + \sin \phi |2\rangle$  are such that  $\langle v | \hat{O} | v \rangle = 7/4$  and  $\langle u | v \rangle = 0$ . Which of the following are possible values of  $\theta$  and  $\phi$  ?

1.  $\theta = -\frac{\pi}{6}$  and  $\phi = \frac{\pi}{3}$
2.  $\theta = \frac{\pi}{6}$  and  $\phi = \frac{\pi}{3}$
3.  $\theta = -\frac{\pi}{4}$  and  $\phi = \frac{\pi}{4}$
4.  $\theta = \frac{\pi}{3}$  and  $\phi = -\frac{\pi}{6}$

**Q2. [June 2015] . 3.5 marks**

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2015 June	3.5 M
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The wavefunction of a particle in onedimension is denoted by  $\psi(x)$  in the coordinate representation and by  $\phi(p) = \int \psi(x)e^{-ipx/\hbar} dx$  in the momentum representation. If the action of an operator  $\hat{T}$  on  $\psi(x)$  is given by  $\hat{T}\psi(x) = \psi(x + a)$ , where  $a$  is a constant, then  $\hat{T}\phi(p)$  is given by

1.  $-\frac{i}{\hbar} ap\phi(p)$
2.  $e^{-iap/\hbar}\phi(p)$
3.  $e^{+iap/\hbar}\phi(p)$
4.  $\left(1 + \frac{i}{\hbar} ap\right)\phi(p)$

**Q3. [June 2015] . 3.5 marks**

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2015 June	3.5 M
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A particle moves in one dimension in the potential

$V = \frac{1}{2}k(t)x^2$ , where  $k(t)$  is a time dependent

parameter. Then  $\frac{d}{dt}\langle V \rangle$ , the rate of change of the expectation value  $\langle V \rangle$  of the potential energy, is

1.  $\frac{1}{2} \frac{dk}{dt} \langle x^2 \rangle + \frac{k}{2m} \langle xp + px \rangle$
2.  $\frac{1}{2} \frac{dk}{dt} \langle x^2 \rangle + \frac{1}{2m} \langle p^2 \rangle$
3.  $\frac{k}{2m} \langle xp + px \rangle$
4.  $\frac{1}{2} \frac{dk}{dt} \langle x^2 \rangle$

**Q4. [June 2015] . 5.0 marks**

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2015 June	5 M
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A particle of mass  $m$  is in a potential  $V = \frac{1}{2} m\omega^2 x^2$ ,

where  $\omega$  is a constant. Let  $\hat{a} = \sqrt{\frac{m\omega}{2\hbar}} \left( \hat{x} + \frac{i\hat{p}}{m\omega} \right)$ . In

the Heisenberg picture  $\frac{d\hat{a}}{dt}$  is given by

1.  $\omega\hat{a}$
2.  $-i\omega\hat{a}$
3.  $\omega\hat{a}^\dagger$
4.  $i\omega\hat{a}^\dagger$

**Q5. [June 2015] . 5.0 marks**

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2015 June	5 M
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Two different sets of orthogonal basis vectors

$\left\{ \begin{pmatrix} 1 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 1 \end{pmatrix} \right\}$  and  $\left\{ \frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ 1 \end{pmatrix}, \frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ -1 \end{pmatrix} \right\}$  are given for a two-

dimensional real vector space. The matrix

representation of a linear operator  $\hat{A}$  in these bases are related by a unitary transformation. The unitary matrix may be chosen to be

1.  $\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$
2.  $\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$
3.  $\frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix}$
4.  $\frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 0 \\ 1 & 1 \end{pmatrix}$

**Q6. [Dec 2016] . 3.5 marks**

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2016 Dec	3.5M
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Consider the two lowest normalized energy eigenfunctions  $\psi_0(x)$  and  $\psi_1(x)$  of a one dimensional system. They satisfy  $\psi_0(x) = \psi_0^*(x)$  and  $\psi_1(x) = \alpha \frac{d\psi_0}{dx}$ , where  $\alpha$  is a real constant. The expectation value of the momentum operator in the state  $\psi_1$  is

1.  $-\frac{\hbar}{\alpha^2}$

2. 0

3.  $\frac{\hbar}{\alpha^2}$

4.  $\frac{2\hbar}{\alpha^2}$

**Q7. [Dec 2016] . 3.5 marks**

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2016 Dec	3.5M
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Consider the operator  $a = x + \frac{d}{dx}$  acting on smooth functions of  $x$ . The commutator  $[a, \cos x]$  is

1.  $-\sin x$
2.  $\cos x$
3.  $-\cos x$
4. 0

**Q8. [June 2016] . 3.5 marks**

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2016 June	3.5M
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The eigenstates corresponding to eigenvalues  $E_1$  and  $E_2$  of a time-independent Hamiltonian are  $|1\rangle$  and  $|2\rangle$  respectively. If at  $t = 0$ , the system is in a state  $|\psi(t = 0)\rangle = \sin\theta|1\rangle + \cos\theta|2\rangle$  the value of  $\langle\psi(t) | \psi(t)\rangle$  at time  $t$  will be

1. 1
2.  $(E_1 \sin^2\theta + E_2 \cos^2\theta) / \sqrt{E_1^2 + E_2^2}$
3.  $e^{iE_1 t/\hbar} \sin\theta + e^{iE_2 t/\hbar} \cos\theta$
4.  $e^{-iE_1 t/\hbar} \sin^2\theta + e^{-iE_2 t/\hbar} \cos^2\theta$

**Q9. [June 2016] . 5.0 marks**

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2016 June	5M
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Consider a gas of Cs atoms at a number density of  $10^{12}$  atoms/cc. When the typical inter-particle distance is equal to the thermal de Broglie wavelength of the particles, the temperature of the gas is nearest to (Take the mass of a Cs atom to be  $22.7 \times 10^{-26}$  kg.)

1.  $1 \times 10^{-9}$  K

2.  $7 \times 10^{-5}$  K

3.  $1 \times 10^{-3}$  K

4.  $2 \times 10^{-8}$  K

**Q10. [Dec 2017] . 3.5 marks**

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2017 Dec	3.5M
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The state vector of a one-dimensional simple harmonic oscillator of angular frequency  $\omega$ , at time  $t = 0$ , is given by  $|\psi(0)\rangle = \frac{1}{\sqrt{2}} [ |0\rangle + |2\rangle ]$ , where  $|0\rangle$  and  $|2\rangle$  are the normalized ground state and the second excited state, respectively. The minimum time  $t$  after which the state vector  $|\psi(t)\rangle$  is orthogonal to  $|\psi(0)\rangle$ , is

1.  $\frac{\pi}{2\omega}$
2.  $\frac{2\pi}{\omega}$
3.  $\frac{\pi}{\omega}$
4.  $\frac{4\pi}{\omega}$

## Q11. [Dec 2017] . 3.5 marks

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2017 Dec	3.5M
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The normalized wavefunction in the momentum space of a particle in one dimension is

$$\phi(p) = \frac{\alpha}{p^2 + \beta^2}, \text{ where } \alpha \text{ and } \beta \text{ are real constants.}$$

The uncertainty  $\Delta x$  in measuring its position is

1.  $\sqrt{\pi} \frac{\hbar \alpha}{\beta^2}$
2.  $\sqrt{\pi} \frac{\hbar \alpha}{\beta^3}$
3.  $\frac{\hbar}{\sqrt{2}\beta}$
4.  $\sqrt{\frac{\pi}{\beta}} \frac{\hbar \alpha}{\beta}$

## Q12. [Dec 2017] . 3.5 marks

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2017 Dec	3.5M
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Let  $x$  denote the position operator and  $p$  the canonically conjugate momentum operator of a particle. The commutator

$$\left[ \frac{1}{2m} p^2 + \beta x^2, \frac{1}{m} p^2 + \gamma x^2 \right]$$

where  $\beta$  and  $\gamma$  are constants, is zero if

1.  $\gamma = \beta$
2.  $\gamma = 2\beta$
3.  $\gamma = \sqrt{2}\beta$
4.  $2\gamma = \beta$

## Q13. [Dec 2017] . 5.0 marks

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2017 Dec	5M
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The Hamiltonian of a two-level quantum system is

$H = \frac{1}{2} \hbar \omega \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix}$  possible initial state in which the probability of the system being in that quantum state does not change with time, is

1.  $\begin{pmatrix} \cos \frac{\pi}{4} \\ \sin \frac{\pi}{4} \end{pmatrix}$
2.  $\begin{pmatrix} \cos \frac{\pi}{8} \\ \sin \frac{\pi}{8} \end{pmatrix}$
3.  $\begin{pmatrix} \cos \frac{\pi}{2} \\ \sin \frac{\pi}{2} \end{pmatrix}$
4.  $\begin{pmatrix} \cos \frac{\pi}{6} \\ \sin \frac{\pi}{6} \end{pmatrix}$

## Q14. [June 2018] . 5.0 marks

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2018 June	5M
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At  $t = 0$ , the wavefunction of an otherwise free particle confined between two infinite walls at  $x = 0$

and  $x = L$  is  $\psi(x, t = 0) = \sqrt{\frac{2}{L}} \left( \sin \frac{\pi x}{L} - \sin \frac{3\pi x}{L} \right)$ . Its wave function at a later time  $t = \frac{mL^2}{4\pi\hbar}$  is

1.  $\sqrt{\frac{2}{L}} \left( \sin \frac{\pi x}{L} - \sin \frac{3\pi x}{L} \right) e^{i\pi/6}$
2.  $\sqrt{\frac{2}{L}} \left( \sin \frac{\pi x}{L} + \sin \frac{3\pi x}{L} \right) e^{-i\pi/6}$
3.  $\sqrt{\frac{2}{L}} \left( \sin \frac{\pi x}{L} - \sin \frac{3\pi x}{L} \right) e^{-i\pi/8}$
4.  $\sqrt{\frac{2}{L}} \left( \sin \frac{\pi x}{L} + \sin \frac{3\pi x}{L} \right) e^{-i\pi/6}$

## Q15. [Dec 2019] . 3.5 marks

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2019 Dec	3.5M
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The energy eigenvalues of a particle of mass  $m$ , confined to a rigid one-dimensional box of width  $L$ , are  $E_n (n = 1, 2, \dots)$ . If the walls of the box are moved very slowly toward each other, the rate of change of time-dependent energy  $\frac{dE_2}{dt}$  of the first excited state is

1.  $\frac{E_2}{L} \frac{dL}{dt}$
2.  $\frac{2E_2}{L} \frac{dL}{dt}$
3.  $-\frac{2E_2}{L} \frac{dL}{dt}$
4.  $-\frac{E_1}{L} \frac{dL}{dt}$

**Q16. [Dec 2019] . 3.5 marks**

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2019 Dec	3.5M
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A particle of mass  $m$  is confined to a box of unit length in one dimension. It is described by the

wavefunction  $\psi(x) = \sqrt{\frac{8}{5}} \sin\pi x(1 + \cos\pi x)$  for

$0 \leq x \leq 1$  and zero outside this interval. The expectation value of energy in this state is

1.  $\frac{4\pi^2}{3m} \hbar^2$
2.  $\frac{4\pi^2}{5m} \hbar^2$
3.  $\frac{2\pi^2}{5m} \hbar^2$
4.  $\frac{8\pi^2}{5m} \hbar^2$

## Q17. [Dec 2019] . 5.0 marks

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2019 Dec	5M
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Let  $\hat{x}$  and  $\hat{p}$  denote position and momentum operators obeying the commutation relation  $[\hat{x}, \hat{p}] = i\hbar$ . If  $|x\rangle$  denotes an eigenstate of  $\hat{x}$  corresponding to the eigenvalue  $x$ , then  $e^{ia\hat{p}/\hbar}|x\rangle$  is

1. an eigenstate of  $\hat{x}$  corresponding to the eigenvalue  $x$
2. an eigenstate of  $\hat{x}$  corresponding to the eigenvalue  $(x + a)$
3. an eigenstate of  $\hat{x}$  corresponding to the eigenvalue  $(x - a)$
4. not an eigenstate of  $\hat{x}$

Q18. [Dec 2019] . 5.0 marks

Quantum Mechanics > Basic Quantum Mechanics

CSIR NET	2019 Dec	5M
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Let the normalized eigenstates of the Hamiltonian

$$H = \begin{pmatrix} 2 & 1 & 0 \\ 1 & 2 & 0 \\ 0 & 0 & 2 \end{pmatrix} \text{ be } |\psi_1\rangle, |\psi_2\rangle \text{ and } |\psi_3\rangle. \text{ The}$$

expectation value  $\langle H \rangle$  and the variance of  $H$  in the

state  $|\psi\rangle = \frac{1}{\sqrt{3}} (|\psi_1\rangle + |\psi_2\rangle - i|\psi_3\rangle)$  are

1.  $\frac{4}{3}$  and  $\frac{1}{3}$
2.  $\frac{4}{3}$  and  $\frac{2}{3}$
3. 2 and  $\frac{2}{3}$
4. 2 and 1

**Q19. [June 2019] . 5.0 marks**

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2019 June	5M
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The wave number  $k$  and the angular frequency  $\omega$  of a wave are related by the dispersion relation

$\omega^2 = \alpha k + \beta k^3$  where  $\alpha$  and  $\beta$  are positive constants. The wave number for which the phase velocity equals the group velocity, is

1.  $3 \sqrt{\frac{\alpha}{\beta}}$

2.  $\sqrt{\frac{\alpha}{\beta}}$

3.  $\frac{1}{2} \sqrt{\frac{\alpha}{\beta}}$

4.  $\frac{1}{3} \sqrt{\frac{\alpha}{\beta}}$

**Q20. [June 2019] . 5.0 marks**

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2019 June	5M
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The operator  $A$  has a matrix representation  $\begin{pmatrix} 2 & 1 \\ 1 & 2 \end{pmatrix}$  in the basis spanned by  $\begin{pmatrix} 1 \\ 0 \end{pmatrix}$  and  $\begin{pmatrix} 0 \\ 1 \end{pmatrix}$ . In another basis spanned by  $\frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ 1 \end{pmatrix}$  and  $\frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ -1 \end{pmatrix}$ , the matrix representation of  $A$  is

1.  $\begin{pmatrix} 2 & 0 \\ 0 & 2 \end{pmatrix}$
2.  $\begin{pmatrix} 3 & 0 \\ 0 & 1 \end{pmatrix}$
3.  $\begin{pmatrix} 3 & 1 \\ 0 & 1 \end{pmatrix}$
4.  $\begin{pmatrix} 3 & 0 \\ 1 & 1 \end{pmatrix}$

**Q21. [June 2019] . 5.0 marks**

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2019 June	5M
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The operator  $x \frac{d}{dx} \delta(x)$ , where  $\delta(x)$  is the Dirac delta function, acts on the space of real valued square-integrable functions on the real line. This operator is equivalent to

1.  $-\delta(x)$
2.  $\delta(x)$
3.  $x$
4.  $0$

**Q22. [June 2020] . 3.5 marks**

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2020 June	3.5M
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Let  $|n\rangle$  denote the energy eigenstates of a particle in a one-dimensional simple harmonic potential

$V(x) = \frac{1}{2} m\omega^2 x^2$ . If the particle is initially prepared

in the state  $|\psi(t = 0)\rangle = \frac{1}{\sqrt{2}} (|0\rangle + |1\rangle)$ , the

minimum time after which the oscillator will be found in the same state is

1.  $3\pi/(2\omega)$
2.  $\pi/\omega$
3.  $\pi/(2\omega)$
4.  $2\pi/\omega$

**Q23. [June 2021] . 3.5 marks**

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2021 June	3.5M
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A two-state system evolves under the action of the Hamiltonian  $H = E_0|A\rangle\langle A| + (E_0 + \Delta)|B\rangle\langle B|$ , where  $|A\rangle$  and  $|B\rangle$  are its two orthonormal states. These states transform to one another under parity, i.e.  $P|A\rangle = |B\rangle$  and  $P|B\rangle = |A\rangle$ . If at time  $t = 0$  the system is in a state of definite parity  $P = 1$ , the earliest time  $t$  at which the probability of finding the system in a state of parity  $P = -1$  is one is

1.  $\frac{\pi\hbar}{2\Delta}$
2.  $\frac{\pi\hbar}{\Delta}$
3.  $\frac{3\pi\hbar}{2\Delta}$
4.  $\frac{2\pi\hbar}{\Delta}$

**Q24. [June 2021] . 5.0 marks**

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2021 June	5M
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The unnormalized wave function of a particle in one dimension in an infinite square well with walls at  $x = 0$  and  $x = a$ , is  $\psi(x) = x(a - x)$ . If  $\psi(x)$  is expanded as a linear combination of the energy eigenfunctions,  $\int_0^a |\psi(x)|^2 dx$  is proportional to the infinite series

(You may use  $\int_0^a t \sin t dt = -a \cos a + \sin a$  and  $\int_0^a t^2 \sin t dt = -2 - (a^2 - 2) \cos a + 2a \sin a$ )

1.  $\sum_{n=1}^{\infty} (2n - 1)^{-6}$
2.  $\sum_{n=1}^{\infty} (2n - 1)^{-4}$
3.  $\sum_{n=1}^{\infty} (2n - 1)^{-2}$
4.  $\sum_{n=1}^{\infty} (2n - 1)^{-8}$

**Q25. [June 2022] . 3.5 marks**

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2022 June	3.5M
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If the expectation value of the momentum of a particle in one dimension is zero, then its (box-normalizable) wave function may be of the form

1.  $\sin kx$
2.  $e^{ikx} \sin kx$
3.  $e^{ikx} \cos kx$
4.  $\sin kx + e^{ikx} \cos kx$

**Q26. [June 2022] . 3.5 marks**

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2022 June	3.5M
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In terms of a complete set of orthonormal basis kets  $|n\rangle$ ,  $n = 0, \pm 1, \pm 2, \dots$ , the Hamiltonian is

$$H = \sum_n (E|n\rangle\langle n| + \epsilon|n+1\rangle\langle n| + \epsilon|n\rangle\langle n+1|)$$

where  $E$  and  $\epsilon$  are constants. The state

$|\varphi\rangle = \sum_n e^{in\varphi} |n\rangle$  is an eigenstate with energy

1.  $E + \epsilon \cos \varphi$
2.  $E - \epsilon \cos \varphi$
3.  $E + 2\epsilon \cos \varphi$
4.  $E - 2\epsilon \cos \varphi$

## Q27. [June 2022] . 3.5 marks

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2022 June	3.5M
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The momentum space representation of the Schrodinger equation of a particle in a potential

$$V(\vec{r}) \quad \text{is} \quad \left( |\vec{p}|^2 + \beta (\nabla_p^2)^2 \right) \psi(\vec{p}, t) = i\hbar \frac{\partial}{\partial t} \psi(\vec{p}, t) ,$$

where  $(\nabla_p)_i = \frac{\partial}{\partial p_i}$ , and  $\beta$  is a constant. The potential is (in the following  $V_0$  and  $a$  are constants)

1.  $V_0 e^{-r^2/a^2}$
2.  $V_0 e^{-r^4/a^4}$
3.  $V_0 \left(\frac{r}{a}\right)^2$
4.  $V_0 \left(\frac{r}{a}\right)^4$

Q28. [Dec 2023] . 5.0 marks

Quantum Mechanics > Basic Quantum Mechanics

CSIR NET	2023 Dec	5 M
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In a quantum harmonic oscillator problem,  $\hat{a}$  and  $\hat{N}$  are the annihilation operator and the number operator, respectively. The operator  $e^{\hat{N}} \hat{a} e^{-\hat{N}}$  is

1.  $\hat{a}$
2.  $e^{-1} \hat{a}$
3.  $e^{-(\hat{I} + \hat{a})}$
4.  $e^{\hat{a}}$

(where  $\hat{I}$  is the identity operator)

**Q29. [June 2023] . 5.0 marks**

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2023 June	5M
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Two operators  $A$  and  $B$  satisfy the commutation relations  $[H, A] = -\hbar\omega B$  and  $[H, B] = \hbar\omega A$ , where  $\omega$  is a constant and  $H$  is the Hamiltonian of the system. The expectation value  $\langle A \rangle_{\psi}(t) = \langle \psi | A | \psi \rangle$  in a state  $|\psi\rangle$ , such that at time  $t = 0$ ,  $\langle A \rangle_{\psi}(0) = 0$  and  $\langle B \rangle_{\psi}(0) = i$ , is

1.  $\sin(\omega t)$
2.  $\sinh(\omega t)$
3.  $\cos(\omega t)$
4.  $\cosh(\omega t)$

**Q30. [Dec 2024] . 5.0 marks**

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2024 Dec	5M
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The constant  $B$  which makes  $e^{-ax^2}$  an eigenfunction of the operator  $\left(\frac{d^2}{dx^2} - Bx^2\right)$  is

1.  $4a^2$
2. 0
3.  $2a$
4. 1

**Q31. [June 2024] . 3.5 marks**

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2024 June	3.5M
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If  $A$  and  $B$  are Hermitian operators and  $C$  is an antihermitian operator, then

1.  $[[A, B], C]$  is hermitian and  $[[A, C], B]$  is antihermitian
2.  $[[A, B], C]$  and  $[[A, C], B]$  are both antihermitian
3.  $[[A, B], C]$  and  $[[A, C], B]$  are both hermitian
4.  $[[A, B], C]$  is antihermitian and  $[[A, C], B]$  is Hermitian

## Q32. [Dec 2025] . 3.5 marks

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2025 Dec	3.5M	QM
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A quantum mechanical particle in a harmonic potential has the wave function  $\frac{1}{\sqrt{2}} [\psi_0(x) + \psi_1(x)]$  at  $t = 0$ , where  $\psi_0(x)$  and  $\psi_1(x)$  are the wave functions of the ground state and the first excited state respectively. If the frequency of the oscillator is  $\omega$ , the probability density of finding the particle at  $x$  after time  $t = \frac{\pi}{\omega}$  is

1.  $\frac{1}{2} |\psi_1(x) - \psi_0(x)|^2$
2.  $\frac{1}{2} |\psi_1(x) + \psi_0(x)|^2$
3.  $\frac{1}{2} |\psi_1(x) - i\psi_0(x)|^2$
4.  $\frac{1}{2} |\psi_1(x)|^2 + \frac{1}{2} |\psi_0(x)|^2$

**Q33. [Dec 2025] . 5.0 marks**

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2025 Dec	5M	QM
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A one-dimensional quantum harmonic oscillator with frequency  $\omega$  is in its ground state. Its normalized wave function is given by

$$\psi(x) = \left(\frac{m\omega}{\pi\hbar}\right)^{\frac{1}{4}} \exp\left[-\frac{m\omega}{2\hbar}x^2\right].$$

The frequency is suddenly increased to  $2\omega$ . The probability of finding the particle in its new ground state is

1.  $\frac{2\sqrt{2}}{3}$
2.  $\left(\frac{2\sqrt{2}}{3}\right)^{\frac{1}{2}}$
3.  $\frac{2}{3}$
4.  $\left(\frac{3}{2\sqrt{2}}\right)^{\frac{1}{2}}$

**Q34. [June 2025] . 3.5 marks**

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2025 June	3.5M	QM
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A particle of mass  $m$  is in the third energy eigenstate of an infinite potential well of width  $a$ . The time interval in which the phase of this wave function changes by  $2\pi$  is

1.  $\frac{4ma^2}{3\pi\hbar}$

2.  $\frac{4ma^2}{9\pi\hbar}$

3.  $\frac{8ma^2}{3\pi\hbar}$

4.  $\frac{8ma^2}{9\pi\hbar}$

**Q35. [June 2025] . 3.5 marks**

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2025 June	3.5M	QM
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The Hamiltonian of the 1-dimensional quantum

harmonic oscillator is given by  $H = \frac{p^2}{2m} + \frac{1}{2}m\omega^2 x^2$ .

The expectation value of  $[D, H]$  in the ground state,

where  $D = \frac{1}{2\hbar}(xp + px)$ , is (in units of  $\hbar\omega$ )

1.  $i$
2.  $\frac{1}{2}$
3.  $\frac{-3i}{2}$
4. 0

**Q36. [June 2025] . 5.0 marks**

Quantum Mechanics &gt; Basic Quantum Mechanics

CSIR NET	2025 June	5M	QM
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The probability density of a free particle of mass  $m$  at time  $t = 0$ , is given by  $A \exp\left(-\frac{x^2}{2\sigma^2(0)}\right)$ . At  $t > 0$ , its probability density is proportional to  $\exp\left(-\frac{x^2}{2\sigma^2(t)}\right)$ , where  $\sigma^2(t)$  is

1.  $\sigma^2(0) + \frac{\hbar^2 t^2}{\sigma^2(0)m^2}$
2.  $\sigma^2(0) + \frac{\hbar^2 t^2}{4\sigma^2(0)m^2}$
3.  $\sigma^2(0) + \frac{4\hbar^2 t^2}{\sigma^2(0)m^2}$
4.  $\sigma^2(0) + \frac{2\hbar^2 t^2}{\sigma^2(0)m^2}$

## Answer Key

36 questions . Subject and topic for quick revision

Q. No	Subject	Topic	Answer
Q1	Quantum Mechanics	Basic Quantum Mechanics	1
Q2	Quantum Mechanics	Basic Quantum Mechanics	3
Q3	Quantum Mechanics	Basic Quantum Mechanics	1
Q4	Quantum Mechanics	Basic Quantum Mechanics	2
Q5	Quantum Mechanics	Basic Quantum Mechanics	3
Q6	Quantum Mechanics	Basic Quantum Mechanics	2
Q7	Quantum Mechanics	Basic Quantum Mechanics	1
Q8	Quantum Mechanics	Basic Quantum Mechanics	1
Q9	Quantum Mechanics	Basic Quantum Mechanics	4
Q10	Quantum Mechanics	Basic Quantum Mechanics	1
Q11	Quantum Mechanics	Basic Quantum Mechanics	3
Q12	Quantum Mechanics	Basic Quantum Mechanics	2
Q13	Quantum Mechanics	Basic Quantum Mechanics	2
Q14	Quantum Mechanics	Basic Quantum Mechanics	4
Q15	Quantum Mechanics	Basic Quantum Mechanics	3
Q16	Quantum Mechanics	Basic Quantum Mechanics	2
Q17	Quantum Mechanics	Basic Quantum Mechanics	3
Q18	Quantum Mechanics	Basic Quantum Mechanics	3
Q19	Quantum Mechanics	Basic Quantum Mechanics	2
Q20	Quantum Mechanics	Basic Quantum Mechanics	2
Q21	Quantum Mechanics	Basic Quantum Mechanics	1
Q22	Quantum Mechanics	Basic Quantum Mechanics	4
Q23	Quantum Mechanics	Basic Quantum Mechanics	2
Q24	Quantum Mechanics	Basic Quantum Mechanics	1
Q25	Quantum Mechanics	Basic Quantum Mechanics	1
Q26	Quantum Mechanics	Basic Quantum Mechanics	3
Q27	Quantum Mechanics	Basic Quantum Mechanics	4
Q28	Quantum Mechanics	Basic Quantum Mechanics	2
Q29	Quantum Mechanics	Basic Quantum Mechanics	2
Q30	Quantum Mechanics	Basic Quantum Mechanics	1
Q31	Quantum Mechanics	Basic Quantum Mechanics	2
Q32	Quantum Mechanics	Basic Quantum Mechanics	1
Q33	Quantum Mechanics	Basic Quantum Mechanics	1
Q34	Quantum Mechanics	Basic Quantum Mechanics	2
Q35	Quantum Mechanics	Basic Quantum Mechanics	4
Q36	Quantum Mechanics	Basic Quantum Mechanics	2

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