

# PhysicsByAaryan

CSIR NET . GATE . JEST . BARC - Physics

## Ordinary Differential Equations - CSIR NET Physics PYQs

Mathematical Physics . All PYQs (2015-2025) with answer key

**13 questions . Answer key included**

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## Q1. [Dec 2015] . 3.5 marks

Mathematical Physics &gt; Ordinary Differential Equations

CSIR NET	2015 Dec	3.5 M
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The solution of the differential equation  $\frac{dx}{dt} = 2\sqrt{1-x^2}$ , with initial condition  $x = 0$  at  $t = 0$  is

1.  $x = \begin{cases} \sin 2t, & 0 \leq t < \frac{\pi}{4} \\ \sinh 2t, & t \geq \frac{\pi}{4} \end{cases}$

2.  $x = \begin{cases} \sin 2t, & 0 \leq t < \frac{\pi}{2} \\ 1, & t \geq \frac{\pi}{2} \end{cases}$

3.  $x = \begin{cases} \sin 2t, & 0 \leq t < \frac{\pi}{4} \\ 1, & t \geq \frac{\pi}{4} \end{cases}$

4.  $x = 1 - \cos 2t, t \geq 0$

**Q2. [June 2015] . 3.5 marks**

Mathematical Physics &gt; Ordinary Differential Equations

CSIR NET	2015 June	3.5 M
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Consider the differential equation

$\frac{d^2x}{dt^2} - 3\frac{dx}{dt} + 2x = 0$ . If  $x = 0$  at  $t = 0$  and  $x = 1$  at  $t = 1$ , the value of  $x$  at  $t = 2$  is

1.  $e^2 + 1$
2.  $e^2 + e$
3.  $e + 2$
4.  $2e$

**Q3. [Dec 2017] . 3.5 marks**

Mathematical Physics &gt; Ordinary Differential Equations

CSIR NET	2017 Dec	3.5M
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The number of linearly independent power series solutions, around  $x = 0$ , of the second order linear differential equation  $x \frac{d^2y}{dx^2} + \frac{dy}{dx} + xy = 0$ , is

1. 0 (this equation does not have a power series solution)
2. 1
3. 2
4. 3

**Q4. [June 2017] . 3.5 marks**

Mathematical Physics &gt; Ordinary Differential Equations

CSIR NET	2017 June	3.5M
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The function  $y(x)$  satisfies the differential equation

$$x \frac{dy}{dx} + 2y = \frac{\cos \pi x}{x}. \text{ If } y(1) = 1, \text{ the value of } y(2) \text{ is}$$

1.  $\pi$
2. 1
3.  $1/2$
4.  $1/4$

**Q5. [Dec 2018] . 3.5 marks**

Mathematical Physics &gt; Ordinary Differential Equations

CSIR NET	2018 Dec	3.5M
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In terms of arbitrary constants  $A$  and  $B$ , the general solution to the differential equation

$$x^2 \frac{d^2 y}{dx^2} + 5x \frac{dy}{dx} + 3y = 0 \text{ is}$$

1.  $y = \frac{A}{x} + Bx^3$
2.  $y = Ax + \frac{B}{x^3}$
3.  $y = Ax + Bx^3$
4.  $y = \frac{A}{x} + \frac{B}{x^3}$

**Q6. [June 2018] . 3.5 marks**

Mathematical Physics &gt; Ordinary Differential Equations

CSIR NET	2018 June	3.5M
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Consider the following ordinary differential equation

$$\frac{d^2x}{dt^2} + \frac{1}{x} \left( \frac{dx}{dt} \right)^2 - \frac{dx}{dt} = 0$$

with the boundary conditions  $x(t = 0) = 0$  and  $x(t = 1) = 1$ . The value of  $x(t)$  at  $t = 2$  is

1.  $\sqrt{e - 1}$
2.  $\sqrt{e^2 + 1}$
3.  $\sqrt{e + 1}$
4.  $\sqrt{e^2 - 1}$

**Q7. [June 2019] . 3.5 marks**

Mathematical Physics &gt; Ordinary Differential Equations

CSIR NET	2019 June	3.5M
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The solution of the differential equation

$x \frac{dy}{dx} + (1+x)y = e^{-x}$  with the boundary condition  $y(x=1) = 0$ , is

1.  $\frac{(x-1)}{x} e^{-x}$
2.  $\frac{(x-1)}{x^2} e^{-x}$
3.  $\frac{(1-x)}{x^2} e^{-x}$
4.  $(x-1)^2 e^{-x}$

**Q8. [June 2020] . 5.0 marks**

Mathematical Physics &gt; Ordinary Differential Equations

CSIR NET	2020 June	5M
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The solution of the differential equation  $\left(\frac{dy}{dx}\right)^2 - \frac{d^2y}{dx^2} = e^y$ , with the boundary conditions  $y(0) = 0$  and  $y'(0) = -1$ , is

1.  $-\ln\left(\frac{x^2}{2} + x + 1\right)$
2.  $-x \ln(e+x)$
3.  $-xe^{-x^2}$
4.  $-x(x+1)e^{-x}$

**Q9. [June 2021] . 3.5 marks**

Mathematical Physics &gt; Ordinary Differential Equations

CSIR NET	2021 June	3.5M
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The equation of motion of a one-dimensional forced harmonic oscillator in the presence of a dissipative force is described by  $\frac{d^2x}{dt^2} + 10 \frac{dx}{dt} + 16x = 6te^{-8t} + 4t^2e^{-2t}$ . The general form of the particular solution, in terms of constants A, B etc., is

1.  $t(At^2 + Bt + C)e^{-2t} + (Dt + E)e^{-8t}$
2.  $(At^2 + Bt + C)e^{-2t} + (Dt + E)e^{-8t}$
3.  $t(At^2 + Bt + C)e^{-2t} + t(Dt + E)e^{-8t}$
4.  $(At^2 + Bt + C)e^{-2t} + t(Dt + E)e^{-8t}$

## Q10. [Dec 2023] . 5.0 marks

Mathematical Physics &gt; Ordinary Differential Equations

CSIR NET	2023 Dec	5 M
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The solution  $y(x)$  of the differential equation

$$y'' + \frac{y}{4} = \frac{x}{2}, \text{ where } 0 \leq x \leq \pi, \text{ together with the}$$

boundary conditions  $y(0) = y(\pi) = 0$  is

1.  $\frac{2}{\pi} \sum_{n=1}^{\infty} (-1)^n \frac{\pi \sin nx}{n \frac{1-n^2}{4}}$

2.  $\frac{2}{\pi} \sum_{n=1}^{\infty} (-1)^n \frac{\pi \sin nx}{2n \frac{1-n^2}{4}}$

3.  $\frac{2}{\pi} \sum_{n=1}^{\infty} (-1)^{n+1} \frac{\pi \sin nx}{n \frac{1-n^2}{4}}$

4.  $\frac{2}{\pi} \sum_{n=1}^{\infty} (-1)^{n+1} \frac{\pi \sin nx}{2n \frac{1-n^2}{4}}$

## Q11. [June 2024] . 5.0 marks

Mathematical Physics &gt; Ordinary Differential Equations

CSIR NET	2024 June	5M
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The general solution for the second order differential equation

$$\frac{d^2y}{dx^2} - y = x \sin x$$

will be

1.  $C_1 e^x + C_2 e^{-x} - \frac{1}{2} (x \sin x + \cos x)$

2.  $C_1 e^x + C_2 e^{-x} - \frac{1}{2} (\sin x - x \cos x)$

3.  $C_1 e^x + C_2 e^{-x} + \frac{1}{2} x (\sin x - \cos x)$

4.  $C_1 e^x + C_2 e^{-x} + \frac{1}{2} x (\sin x + \cos x)$

(where  $C_1$  and  $C_2$  are arbitrary constants)

**Q12. [June 2025] . 3.5 marks**

Mathematical Physics &gt; Ordinary Differential Equations

CSIR NET	2025 June	3.5M	MMP
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The solutions of the differential equation

$$\frac{dy}{dx} = -\frac{x}{y+1}$$

are a family of

1. ellipses with different eccentricities
2. circles with different centres
3. circles with different radii
4. ellipses with different foci

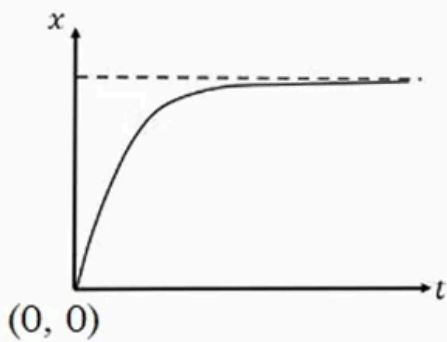
## Q13. [June 2025] . 5.0 marks

Mathematical Physics &gt; Ordinary Differential Equations

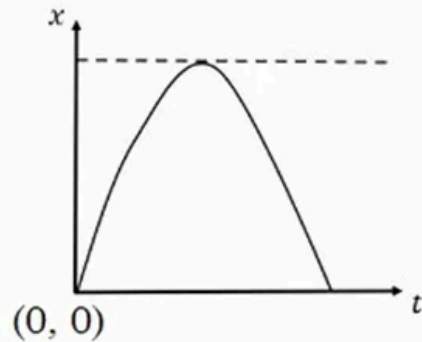
CSIR NET	2025 June	5M	MMP
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Which one of the following curves best represents the solution of the differential equation  $\frac{dx}{dt} + x = 1$ , with the initial condition  $x(0) = 0$  ?

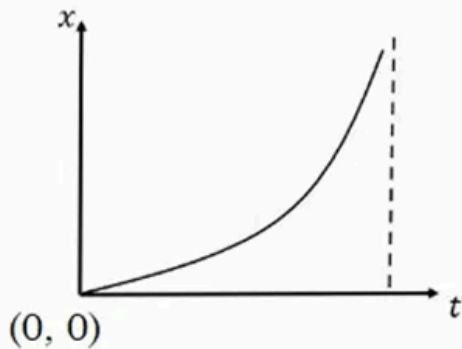
1.



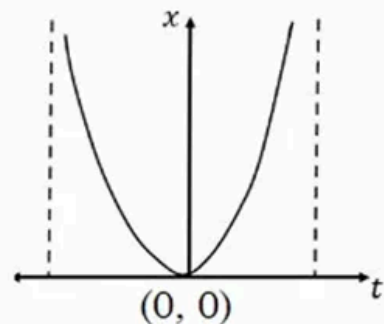
3.



2.



4.



## Answer Key

13 questions . Subject and topic for quick revision

Q. No	Subject	Topic	Answer
Q1	Mathematical Physics	Ordinary Differential Equations	3
Q2	Mathematical Physics	Ordinary Differential Equations	2
Q3	Mathematical Physics	Ordinary Differential Equations	2
Q4	Mathematical Physics	Ordinary Differential Equations	4
Q5	Mathematical Physics	Ordinary Differential Equations	4
Q6	Mathematical Physics	Ordinary Differential Equations	3
Q7	Mathematical Physics	Ordinary Differential Equations	1
Q8	Mathematical Physics	Ordinary Differential Equations	1
Q9	Mathematical Physics	Ordinary Differential Equations	3
Q10	Mathematical Physics	Ordinary Differential Equations	4
Q11	Mathematical Physics	Ordinary Differential Equations	1
Q12	Mathematical Physics	Ordinary Differential Equations	3
Q13	Mathematical Physics	Ordinary Differential Equations	1

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